

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel**  
International  
Advanced Level

Centre Number

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# Wednesday 8 January 2020

Morning (Time: 1 hour 30 minutes)

Paper Reference **WMA11/01**

## Mathematics

**International Advanced Subsidiary/Advanced Level**

**Pure Mathematics P1**

**You must have:**

Mathematical Formulae and Statistical Tables (Lilac), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations.  
Calculators must not have the facility for symbolic algebra manipulation,  
differentiation and integration, or have retrievable mathematical  
formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need*.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet ‘Mathematical Formulae and Statistical Tables’ is provided.
- There are 11 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question*.

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

**Turn over ▶**

P60796A

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P 6 0 7 9 6 A 0 1 2 8



**Pearson**

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1. Find, in simplest form,

$$\int \left( \frac{8x^3}{3} - \frac{1}{2\sqrt{x}} - 5 \right) dx$$

(4)

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**Question 1 continued**

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Q1

(Total 4 marks)



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2. Given  $y = 3^x$ , express each of the following in terms of  $y$ . Write each expression in its simplest form.

(a)  $3^{3x}$

(1)

(b)  $\frac{1}{3^{x-2}}$

(2)

(c)  $\frac{81}{9^{2-3x}}$

(2)

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**Question 2 continued**

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Q2

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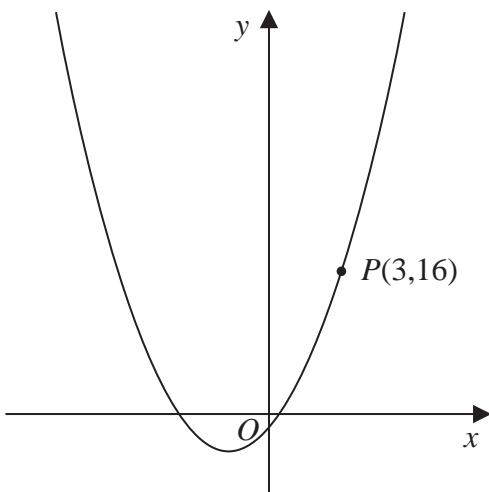
**Figure 1**

Figure 1 shows part of the curve with equation  $y = x^2 + 3x - 2$

The point  $P(3,16)$  lies on the curve.

- (a) Find the gradient of the tangent to the curve at  $P$ .

(2)

The point  $Q$  with  $x$  coordinate  $3 + h$  also lies on the curve.

- (b) Find, in terms of  $h$ , the gradient of the line  $PQ$ . Write your answer in simplest form.

(3)

- (c) Explain briefly the relationship between the answer to (b) and the answer to (a).

(1)

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**Question 3 continued**

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Q3

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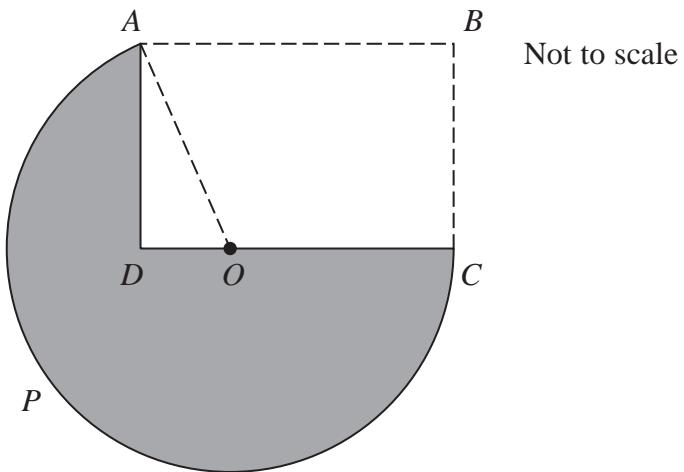
**Figure 2**

Figure 2 shows the plan view of a house  $ABCD$  and a lawn  $APCDA$ .

$ABCD$  is a rectangle with  $AB = 16\text{ m}$ .

$APCOA$  is a sector of a circle centre  $O$  with radius  $12\text{ m}$ .

The point  $O$  lies on the line  $DC$ , as shown in Figure 2.

- (a) Show that the size of angle  $AOD$  is  $1.231$  radians to 3 decimal places. (2)

The lawn  $APCDA$  is shown shaded in Figure 2.

- (b) Find the area of the lawn, in  $\text{m}^2$ , to one decimal place. (4)

- (c) Find the perimeter of the lawn, in metres, to one decimal place. (3)

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### Question 4 continued

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Q4

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5. (a) Find, using algebra, all solutions of

$$20x^3 - 50x^2 - 30x = 0 \quad (3)$$

- (b) Hence find all real solutions of

$$20(y+3)^{\frac{3}{2}} - 50(y+3) - 30(y+3)^{\frac{1}{2}} = 0 \quad (4)$$

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Q5

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6. The line  $l_1$  has equation  $3x - 4y + 20 = 0$

The line  $l_2$  cuts the  $x$ -axis at  $R(8,0)$  and is parallel to  $l_1$

- (a) Find the equation of  $l_2$ , writing your answer in the form  $ax + by + c = 0$ , where  $a$ ,  $b$  and  $c$  are integers to be found.

(3)

The line  $l_1$  cuts the  $x$ -axis at  $P$  and the  $y$ -axis at  $Q$ .

Given that  $PQRS$  is a parallelogram, find

- (b) the area of  $PQRS$ ,

(3)

- (c) the coordinates of  $S$ .

(2)

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Q6

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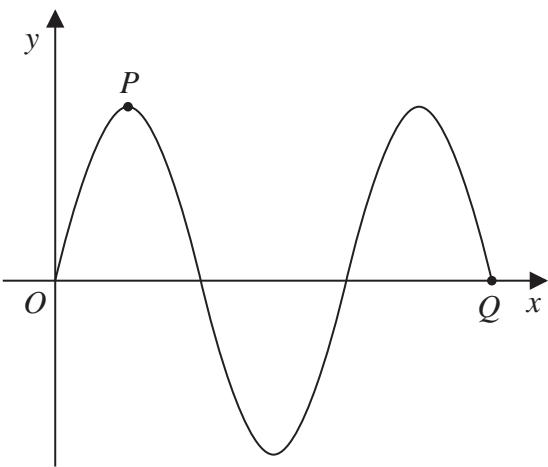
**Figure 3**

Figure 3 shows part of the curve  $C_1$  with equation  $y = 3\sin x$ , where  $x$  is measured in degrees.

The point  $P$  and the point  $Q$  lie on  $C_1$  and are shown in Figure 3.

(a) State

- (i) the coordinates of  $P$ ,
- (ii) the coordinates of  $Q$ .

(3)

A different curve  $C_2$  has equation  $y = 3\sin x + k$ , where  $k$  is a constant.

The curve  $C_2$  has a maximum  $y$  value of 10

The point  $R$  is the minimum point on  $C_2$  with the smallest positive  $x$  coordinate.

(b) State the coordinates of  $R$ .

(2)

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Q7

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8. The straight line  $l$  has equation  $y = k(2x - 1)$ , where  $k$  is a constant.

The curve  $C$  has equation  $y = x^2 + 2x + 11$

Find the set of values of  $k$  for which  $l$  does not cross or touch  $C$ .

(6)

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Q8

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9.

**In this question you must show all stages of your working.**

**Solutions relying on calculator technology are not acceptable.**

A curve has equation

$$y = \frac{4x^2 + 9}{2\sqrt{x}} \quad x > 0$$

Find the  $x$  coordinate of the point on the curve at which  $\frac{dy}{dx} = 0$

(6)

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**Q9**

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- 10.** The curve  $C_1$  has equation  $y = f(x)$ , where

$$f(x) = (4x - 3)(x - 5)^2$$

- (a) Sketch  $C_1$  showing the coordinates of any point where the curve touches or crosses the coordinate axes.

(3)

- (b) Hence or otherwise

(i) find the values of  $x$  for which  $f\left(\frac{1}{4}x\right) = 0$

- (ii) find the value of the constant  $p$  such that the curve with equation  $y = f(x) + p$  passes through the origin.

(2)

A second curve  $C_2$  has equation  $y = g(x)$ , where  $g(x) = f(x + 1)$

- (c) (i) Find, in simplest form,  $g(x)$ . You may leave your answer in a factorised form.

- (ii) Hence, or otherwise, find the  $y$  intercept of curve  $C_2$

(3)

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**Q10**

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11. A curve has equation  $y = f(x)$ , where

$$f''(x) = \frac{6}{\sqrt{x^3}} + x \quad x > 0$$

The point  $P(4, -50)$  lies on the curve.

Given that  $f'(4) = -4$  at  $P$ ,

- (a) find the equation of the normal at  $P$ , writing your answer in the form  $y = mx + c$ , where  $m$  and  $c$  are constants,

(3)

- (b) find  $f(x)$ .

(8)

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**Q11**

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